



TurboRVB and Turbo-Genius: Overview and Workflow

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Day3:

- Single-shot VMC
- VMC force





VMC input file





ngen is the total number of Monte Carlo steps.

Default: nw is the number of MPI processes.





from scipy.io import FortranFile
import numpy as np

```
# check length of fort.12
f = FortranFile('fort.12', 'r')
a = f.read_reals(dtype='float64')
column_length = len(a)
f.close()
```

```
# start reading fort.12
head = ("head", "<i")
tail = ("tail", "<i")
dt = np.dtype([head, ("a", "<{}d".format(column_length)), tail])
fd = open('fort.12', "r")
fort12 = np.fromfile(fd, dtype=dt, count=-1)
data_length=len(fort12)
fd.close()
# end reading fort.12
```

print(fort12)

# for ngen=10		
>>> fort12		
array([(40, [1.	, 1.	, -11.23924971, -11.23924971, 126.32073395], 40),
(40, [1.	, 1.	, -11.4465321 , -11.4465321 , 131.02309712], 40),
(40, [1.	, 1.	, -11.25058355, -11.25058355, 126.57563015], 40),
(40, [1.	, 1.	, -11.88021352, -11.88021352, 141.13947319], 40),
(40, [1.	, 1.	, -10.89686295, -10.89686295, 118.74162225], 40),
(40, [1.	, 1.	, -11.8906161 , -11.8906161 , 141.38675112], 40),
(40, [1.	, 1.	, -10.50040878, -10.50040878, 110.25858451], 40),
(40, [1.	, 1.	, -10.85804034, -10.85804034, 117.89704005], 40),
(40, [1.	, 1.	, -11.3042634 , -11.3042634 , 127.78637111], 40),
(40, [1.	, 1.	, -10.86745849, -10.86745849, 118.10165397], 40)],
<pre>dtype=[('head',</pre>	' <i4'), ('a',<="" td=""><td>'<f8', '<i4')])<="" ('tail',="" (5,)),="" td=""></f8',></td></i4'),>	' <f8', '<i4')])<="" ('tail',="" (5,)),="" td=""></f8',>

e(L), etc... -> written in fort.12



forcevmc.sh "bin", "init", "pulay", or turbo-genius.sh –j vmc -post -reb "bin", -eq "init"

pip0.d=energy

"bin": the length of reblocking size

"init": the length of equilibration steps (init * bin)

"pulay": the ratio of the pulay term (1 is OK)

#cat pip0.d

```
number of bins read =1496Energy = -1.13791927721883271.7589095174214898E-004Variance square =1.7369139136828382E-0032.7618833870090571E-005Est. energy error bar =1.7510470092362484E-0043.9800256121536918E-006Est. corr. time =2.64202665232202080.10738159557488412
```

forcevmc.dat=forces

Force component 1 Force = 6.004763869201490E-003 4.997922374161991E-005 6.273565633363322E-007 Der Eloc = 6.927675852724724E-003 4.999242839793062E-005 <0H> = 0.557134685159244 7.437283601136703E-005 <0><H> = -0.557596141151006 7.447559481785158E-005 2*(<0H> - <0><H>) = -9.229119835232336E-004 2.922997214772288E-006



(i) It employs the Resonating Valence Bond (RVB) WF that includes static and dynamical correlation effects beyond the commonly used Slater determinant, while keeping the computational cost at the single-determinant level.

(ii) The code implements a VMC algorithm based on localized orbitals (e.g., Gaussians) and state-of-the-art optimization methods, such as the stochastic reconfiguration. Therefore, at the VMC level, one can optimize not only the amplitude of the WF (i.e., the Jastrow factor), but also the nodal surfaces (e.g., the Slater determinant). This leads to a better variational energy in general, and also improves the corresponding FN-DMC energy.

(iii) The energy derivatives (e.g., atomic forces) are calculated very efficiently thanks to an implementation based on the Adjoint Algorithmic Differentiation (AAD). As a consequence, one can perform structural optimizations and Langevin molecular dynamics.

(iv) The code implements the newly developed Lattice Regularized Diffusion Monte Carlo (LRDMC), a stable DMC algorithm that, very recently, has shown to have a better scaling with the atomic number Z, compared with standard DMC.

K. Nakano, C. Attaccalite, M. Barborini, L. Capriotti, M. Casula, E. Coccia, M. Dagrada, Y. Luo, G. Mazzola, A. Zen, and S. Sorella, *J. Chem. Phys.* <u>152</u>, 204121 (2020)



VMC input file



ngen is the total number of Monte Carlo steps.

Default: nw is the number of MPI processes.



Ionic Forces:

<pre># Constraints for forces: ion - coordinate 1 1 3</pre>	# The number of forces,	atom index,	direction
F1,z for the first atom will be calcula	ated.		
# Constraints for forces: ion - coordinate 2 1 1 2 -3			
F1,x and F2,z will be calculated, ass	uming, $F = F1, x = -F2$	2,Z.	

The output value (forcevmc.dat) is the sum of two forces, i.e., (F = F1, x - F2, z.)

If you want to calculate forces, please set "ieskin=1" in the ¶meter section in your VMC input.



forcevmc.dat

forcevmc.dat=forces

Force component 1 Force = 6.004763869201490E-003 4.997922374161991E-005 6.273565633363322E-007 Der Eloc = 6.927675852724724E-003 4.999242839793062E-005 <OH> = 0.557134685159244 7.437283601136703E-005 <O><H> = -0.557596141151006 7.447559481785158E-005 2*(<OH> - <O><H>) = -9.229119835232336E-004 2.922997214772288E-006

Force (total)
$$F_{\alpha} = -\left\langle \frac{d}{d\mathbf{R}_{\alpha}} E_L \right\rangle - 2\left(\left\langle E_L \cdot \frac{d}{d\mathbf{R}_{\alpha}} \log(J^{1/2}\Psi) \right\rangle - \left\langle E_L \right\rangle \cdot \left\langle \frac{d}{d\mathbf{R}_{\alpha}} \log(J^{1/2}\Psi) \right\rangle \right),$$

Der Eloc:
$$2^*(\langle \mathsf{OH} \rangle - \langle \mathsf{O} \rangle \langle \mathsf{H} \rangle)$$

(Hellmann-Feynman term)

(Pulay term)

where, J is the Jacobian of the warp transformation. S Sorella, L Capriotti, J. Chem. Phys. 133, 234111 (2010).

Constraints for forces: ion - coordinate
 2 1 1 2 -3

The output value (forcevmc.dat) is the sum of two forces, i.e., (F = F1, x - F2, z.)



Energy derivative v.s. Force

$$\frac{dE}{dR_{\alpha}} = \langle \frac{\partial}{\partial R_{\alpha}} E_L \rangle + 2(\langle E_L \frac{\partial}{\partial R_{\alpha}} \log \Psi \rangle - \langle E_L \rangle \langle \frac{\partial}{\partial R_{\alpha}} \log \Psi \rangle)$$

$$+ \sum_{i=1}^{N_{\text{par}}} \frac{\partial E}{\partial c_i} \frac{\partial c_i}{\partial R_{\alpha}} \quad \text{Additional terms!!} \quad \text{JSD ? } \phi_i^{\mathbf{R}} = \sum_{a,l} \frac{c_{i,\{a,l\}}}{c_{i,\{a,l\}}} \psi_{\{a,l\}}^{R_a}$$
1. The system is already at a variational minimum. $\frac{\partial E}{\partial c_i} = 0 \longrightarrow \text{JAGPs } O$
2. The variational parameters are not allowed to vary with changing the atomic pos. $\frac{\partial c_i}{\partial R_{\alpha}} = 0$

J. Tiihonen et al., *J. Chem. Phys.* 154, 204111 (2021)



All-electron calculations, VMC (JDFT). Jastrow factors were optimized for each C-O distance.



Basis = cc-pVQZ



TurboRVB employs the CRYSTAL periodic basis for PBC calculations:

$$\psi_{l,m,I}^{\text{PBC}}\left(\mathbf{r};\zeta\right) = \sum_{\mathbf{T}_{s}} \psi_{l,m,I}\left(\mathbf{r} + \mathbf{T}_{s};\zeta\right) e^{-i\mathbf{k}_{s}\cdot\mathbf{T}_{s}}$$

-PBC, pseudo potential:

Unfortunately, provided basis sets for open systems are redundant for periodic cases, so we recommend that one should cut several smaller exponents, typically, smaller than 0.10.

-PBC, all-electron:

The same for all-electron cases. Basis sets provided for open systems such as Basis set exchange [https://www.basissetexchange.org] are usually redundant for a periodic case, so we recommend that one should cut several smaller exponents, typically, <u>smaller than 0.10</u>.

One can also use all-electron basis sets optimized for periodic systems such as ones provided in the CRYSTAL DFT code [https://www.crystal.unito.it/basis-sets.php].

Basis set redundancy for periodic cases

Linear dependency = the condition number of the overlap matrix (S).

• Diamond: Total Energy (E)

 Ψ_{SD}

 $\Psi = J$



 R_a



 $\phi_i^{\mathbf{R}} = \sum_{a,l} c_{i,\{a,l\}}$





Only one C is displaced

K. Nakano et al., Phys. Rev. B <u>103</u>, L121110 (2021)



- Diamond: the conventional 2x2x2 supercell with the experimental lattice parameter
- The frozen phonon method implemented in Phonopy package.



A. Togo and I. Tanaka, Scr. Mater. <u>108</u>, 1 (2015).

- Raman Freq. (optical phonon at Γ)							
DFT-LDA	38.55 THz						
VMC	40.65(38) THz						
Exp.	40.35 THz						
** These are harmonic frequencies							

K. Nakano et al., Phys. Rev. B <u>103</u>, L121110 (2021)



			Ansatz Level															
		JDFT			JsAGPs			JAGPu				JAGP(JPf)						
1. H ₂ -dimer	H ₂	<u>01</u> DFT Day1	<u>02</u> VMCo Day2,3	<u>03</u> VMC Day3	<u>04</u> DMC Day4	<u>06</u> Conv. Day2	<u>08</u> VMCo Day2,3	<u>09</u> VMC Day3	<u>10</u> DMC Day4	NA					NA			
2. C ₂ -dimer	C ₂	<u>01-01</u> 01-05	<u>01-06</u> VMCo	<u>01-07</u> VMC	<u>01-08</u> DMC	<u>02-01</u> Conv.	<u>02-02</u> VMCo	<u>02-03</u> VMC	<u>02-04</u> DMC	<u>03-01</u> <u>03-03</u> DFT Day1	<u>03-04</u> 03	03-05	03-06	<u>03-06</u>	<u>04-01</u> Conv. Day3	04-03	04-03	<u>04-03</u>
	С	DFT Day1	Day2,3	Day3	Day4	Day2	Day2,3	Day3	Day4	<u>03-01</u> DFT Day1	Conv. Day2	VMCo Day2,3	VMC Day3	DMC Day4	<u>04-02</u> Conv. Day3	VMCo Day4	Day4	Divic Day4
3. H ₂ on graphene	H ₂ + Graphene	01 DFT Day1	02 VMCo Day2,3	03 VMC Day3	04 DMC Day4	NA												
	Graphene	05 DFT Day1	06 VMCo Day2,3	07 VMC Day3	08 DMC Day4					NA					NA			
	H ₂	09 DFT Day1	10 VMCo Day2, 3	11 VMCo Day3	12 DMC Day4													



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