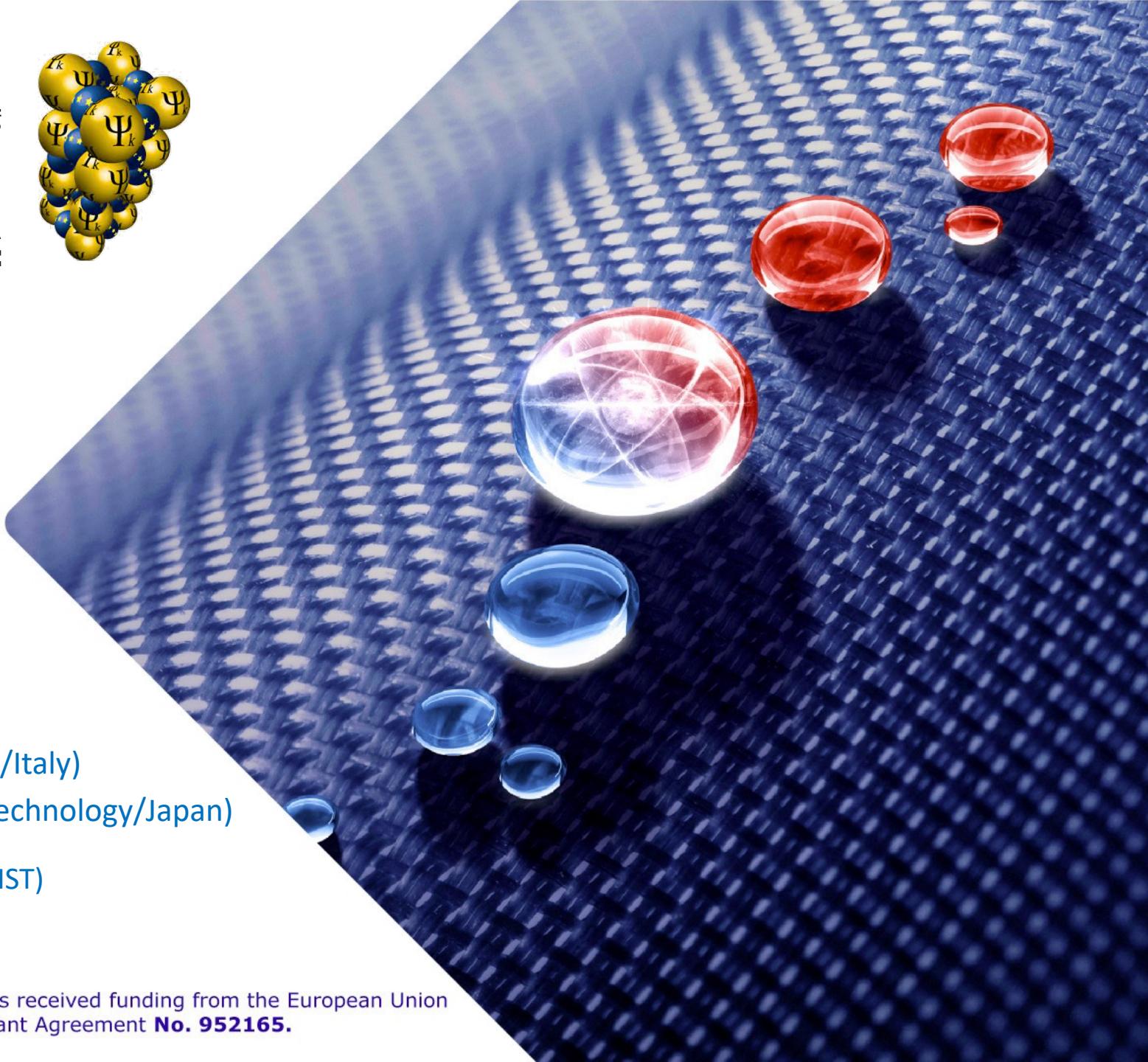


TurboRVB and Turbo-Genius: Overview and Workflow

Kosuke Nakano

- SISSA (International School for Advanced Studies/Italy)
 - JAIST (Japan Advanced Institute of Science and Technology/Japan)
- (Prof. Sorella group/SISSA) (Prof. Maezono group/JAIST)

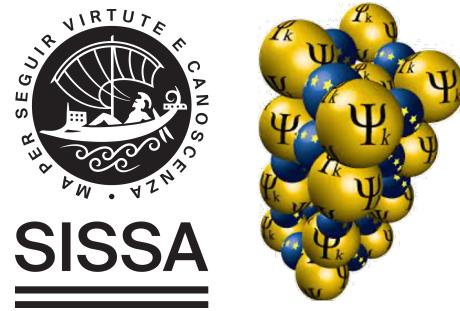


Targeting Real Chemical Accuracy at the Exascale project has received funding from the European Union
Horizon 2020 research and innovation programme under Grant Agreement **No. 952165**.

```
# compilation-and-installation  
# dft  
# general  
# lectures  
# lrdmc  
# random  
# turbo-genius  
# tutorials  
# user-manuals  
# vmc  
# vmc-optimization  
# wf-conversion
```

- Compilation and Installation: Compilations
- DFT: DFT calculations (prep.x)
- VMC: Single-shot VMC, also Force calculations
- VMC-optimization: Optimizations
- LRDMC: LRDMC.
- Turbo-Genius: Turbo-Genius python wrappers
- User manuals and Tutorials.

Others??

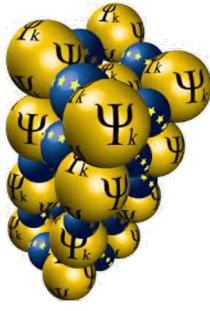
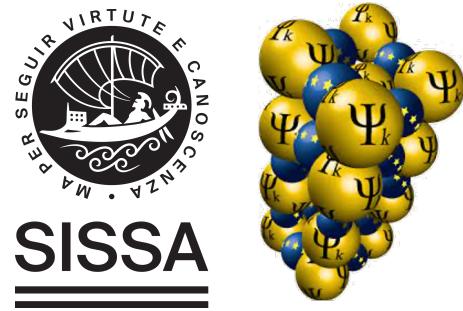


Day2:

- Various ansatz (JDFT/JsAGPs/JAGPu/JAGP)
- Wavefunction conversion
- Wavefunction optimization



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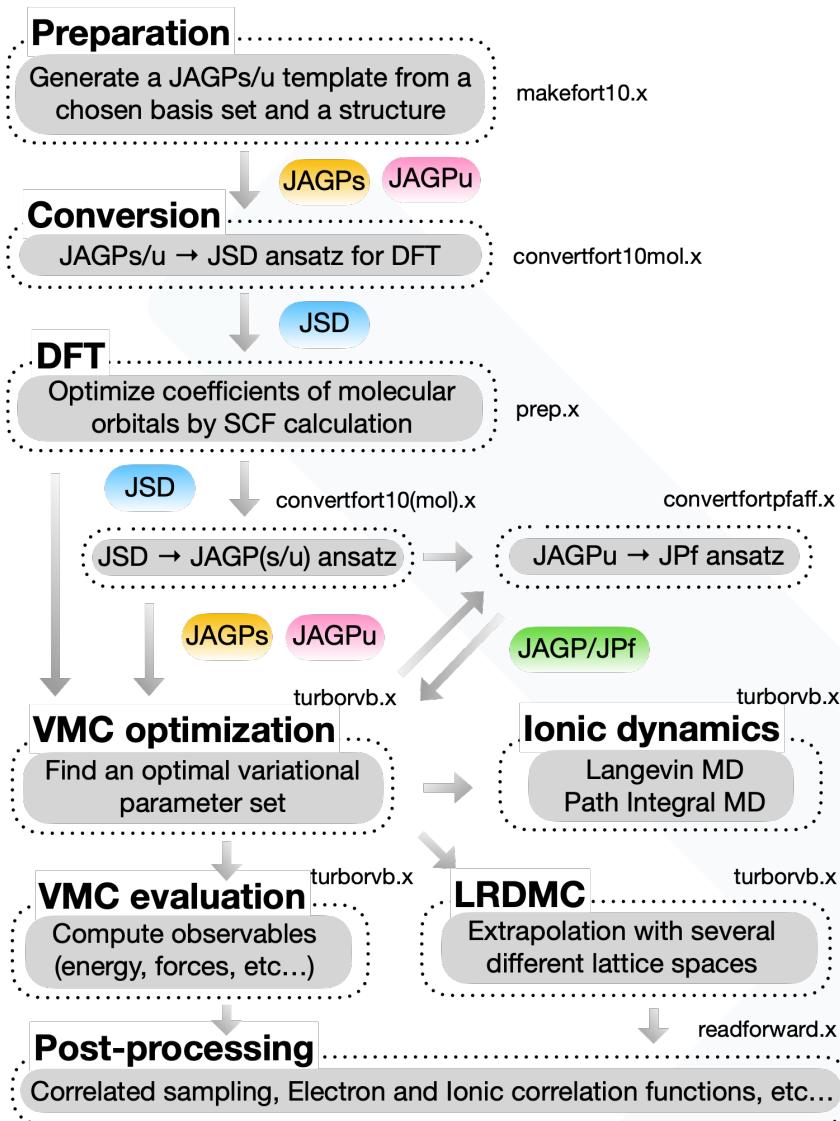


Day2:

- Various ansatz (JDFT/JsAGPs/JAGPu/JAGP)
- Wavefunction conversion
- Wavefunction optimization



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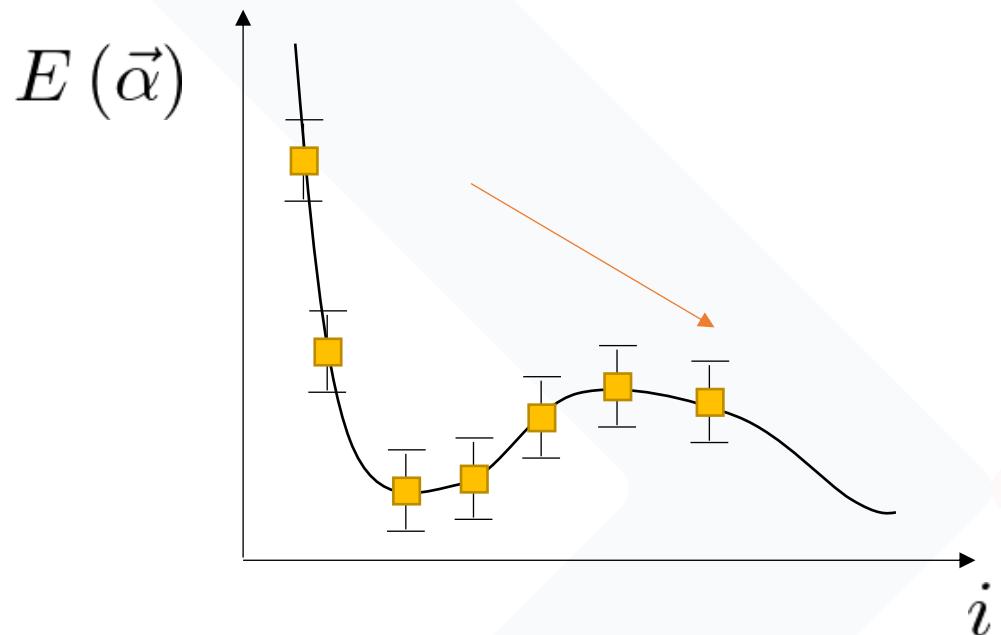


= Workflow =

- ```
graph TD; A[1. Prepare a structure and basis set
makefort10.x
Day1] --> B[2. DFT
Construct a reasonable initial WF!
prep.x
Day1]; B --> C[3. VMC-opt
Optimize the wavefunction
turborvb.x
Day2]; C --> D[4. VMC
Do a VMC run.
turborvb.x
Day3]; D --> E[5. LRDMC
LRDMC with the optimized WF.
turborvb.x
Day4]
```

$$E(\vec{\alpha}) = \frac{\int d\vec{R} \cdot \Psi^*(\vec{R}, \vec{\alpha}) \cdot \hat{\mathcal{H}}\Psi(\vec{R}, \vec{\alpha})}{\int d\vec{R} \cdot \Psi^*(\vec{R}, \vec{\alpha}) \Psi(\vec{R}, \vec{\alpha})} \geq E_0 \quad \text{The variational principle}$$

This integral is evaluated using the MCMC method.



Variational parameters!

$$\vec{\alpha}_{i+1} \leftarrow \vec{\alpha}_i + \Delta \vec{\alpha}$$

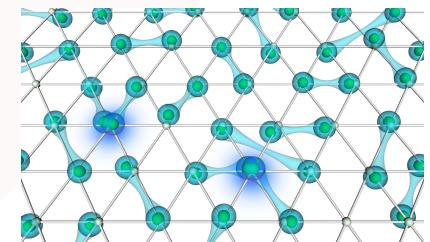
e.g.,

$$f_S(\mathbf{r}_i, \mathbf{r}_j) = \sum_{l,m,a,b} A_{\{a,l\},\{b,m\}} \psi_{a,l}(\mathbf{r}_i) \psi_{b,m}(\mathbf{r}_j).$$

$\Psi(\mathbf{r}_1, \mathbf{r}_2, \dots, \mathbf{r}_N)$  should be anti-symmetric under exchange of electron positions.

Slater determinant: the most straightforward ansatz     $\Psi_{\text{VMC}} = \text{Det} |\phi_1, \phi_2, \dots, \phi_N|$

- ↓
  - Linear combination of the slater determinants.     $\Psi_{\text{VMC}} = \text{Det} |\phi_1, \phi_2, \dots, \phi_N| +$
  - Geminal functions (i.e., considering pairs of electrons.)
  - Backflow functions (i.e., increase in the effective masses of electrons.)
  - Fermi-net (i.e., anti-symmetric neural network.)



c.f. P.W. Anderson

More complex.

The more complex an ansatz is, the better energy we could get. However, the computational cost also increases.

One should increase the number of variational parameters, considering “physics”.

**JAGP/JPf (single+triplet)**

**AGPu (singlet+triplet)**

**AGPs (singlet)**

**SD (singlet + MO)  
Single Slater determinant**

The most general ansatz is represented as the Pfaffian.

$$\Phi_{\text{Pf}} = \text{Pf}(G) \equiv \frac{1}{2^{N/2}(N/2)!} \sum_{P \in S_N} \epsilon_P G_{P(1),P(2)} \cdots G_{P(N-1),P(N)}$$

$$G = \left[ \begin{array}{c|c} G_{uu} & G_{ud} \\ \hline G_{du} & G_{dd} \end{array} \right]$$

$$g_{uu}(\mathbf{i}, \mathbf{j}) = f_{uu}(\mathbf{r}_i, \mathbf{r}_j) |\uparrow\uparrow\rangle \quad g_{dd}(\mathbf{i}, \mathbf{j}) = f_{dd}(\mathbf{r}_i, \mathbf{r}_j) |\downarrow\downarrow\rangle$$

$$g_{ud}(\mathbf{i}, \mathbf{j}) = f_S(\mathbf{r}_i, \mathbf{r}_j) \frac{|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle}{\sqrt{2}} + f_T(\mathbf{r}_i, \mathbf{r}_j) \frac{|\uparrow\downarrow\rangle + |\downarrow\uparrow\rangle}{\sqrt{2}}$$

→ JAGP/JPf

$$\text{Pf} \left( \begin{array}{c|c} 0 & G_{ud} \\ \hline -G_{ud}^T & 0 \end{array} \right) = (-1)^{\frac{N/2 \times (N/2-1)}{2}} \det(G_{ud})$$

$$\Phi_{\text{AGPs/AGPu}} = \det(G_{ud})$$

$$g_{ud}(\mathbf{i}, \mathbf{j}) \equiv g_s(\mathbf{i}, \mathbf{j}) = f_S(\mathbf{r}_i, \mathbf{r}_j) \frac{|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle}{\sqrt{2}}, \quad \rightarrow \text{JAGPs}$$

$$g_{ud}(\mathbf{i}, \mathbf{j}) = f_S(\mathbf{r}_i, \mathbf{r}_j) \frac{|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle}{\sqrt{2}} + f_T(\mathbf{r}_i, \mathbf{r}_j) \frac{|\uparrow\downarrow\rangle + |\downarrow\uparrow\rangle}{\sqrt{2}} \quad \rightarrow \text{JAGPu}$$

Paring functions are parametrized:

$$f(\mathbf{r}_i, \mathbf{r}_j) = \sum_{l,m,a,b} A_{\{a,l\},\{b,m\}} \psi_{a,l}(\mathbf{r}_i) \psi_{b,m}(\mathbf{r}_j)$$

They are not indices for the electrons, but for the basis!!

They are variational parameters, and written in fort.10!!

| # | Nonzero values of detmat |                        |  |
|---|--------------------------|------------------------|--|
| 1 | 5                        | 9.421753101774391E-002 |  |
| 1 | 6                        | 9.421753101774391E-002 |  |
| 1 | 7                        | 9.421753101774391E-002 |  |

## Coefficients of the Determinant part (JAGPs case)

```
Nonzero values of detmat
1 5 9.421753101774391E-002
1 6 9.421753101774391E-002
1 7 9.421753101774391E-002
```

$$A = \begin{pmatrix} A_{11} & A_{12} & \dots & A_{1n} \\ A_{21} & A_{22} & \dots & A_{2n} \\ \vdots & \ddots & \ddots & \vdots \\ & & & A_{nn} \end{pmatrix}$$

$$f(\mathbf{r}_i, \mathbf{r}_j) = \sum_{l,m,a,b} A_{\{a,l\},\{b,m\}} \psi_{a,l}(\mathbf{r}_i) \psi_{b,m}(\mathbf{r}_j)$$

$$g_{ud}(\mathbf{i}, \mathbf{j}) \equiv g_s(\mathbf{i}, \mathbf{j}) = f_S(\mathbf{r}_i, \mathbf{r}_j) \frac{|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle}{\sqrt{2}}, \quad \rightarrow \quad \text{JAGPs}$$

$A_{\{a,l\},\{b,m\}}$  is a symmetric matrix!

## Coefficients of the Determinant part (JAGPu case)

```
Nonzero values of detmat
1 1 8.321544938822982E-001 <- singlet
.....
1 5 9.421753101774391E-002 <- singlet
1 6 9.421753101774391E-002
1 7 9.421753101774391E-002
2 1 3.485892384239842E-003 <- triplet
2 2 3.589529849283749E-001 <- singlet
2 3 2.489548797987997E-002 <- singlet
3 1 1.112333456889842E-003 <- triplet
3 2 2.58577744345490E-001 <- triplet
3 3 3.936485649473937E-002 <- singlet
```

- $A_{\{a,l\},\{b,m\}}$ 
  - is symmetric for the singlet part
  - is skew-symmetric for the triplet part

$$A_S = \begin{pmatrix} A_{11} & A_{12} & \dots & A_{1n} \\ A_{21} & \dots & A_{2n} \\ \ddots & \vdots & & \\ A_{n1} & A_{n2} & \dots & 0 \end{pmatrix} \quad A_T = \begin{pmatrix} 0 & -A_{21} & \dots & -A_{n1} \\ A_{21} & 0 & \dots & -A_{n2} \\ \vdots & \vdots & \ddots & \vdots \\ A_{n1} & A_{n2} & \dots & 0 \end{pmatrix}$$

$$f(\mathbf{r}_i, \mathbf{r}_j) = \sum_{l,m,a,b} A_{\{a,l\},\{b,m\}} \psi_{a,l}(\mathbf{r}_i) \psi_{b,m}(\mathbf{r}_j)$$

$$g_{ud}(\mathbf{i}, \mathbf{j}) = f_S(\mathbf{r}_i, \mathbf{r}_j) \frac{|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle}{\sqrt{2}} + f_T(\mathbf{r}_i, \mathbf{r}_j) \frac{|\uparrow\downarrow\rangle + |\downarrow\uparrow\rangle}{\sqrt{2}}$$

JAGPu

## The most general paring function (Pfaffian ansatz).

```
This is a C2-dimer case
The number of basis set for each carbon is 4
Nonzero values of detmat
1 2 -2.917621798712210E-002 <- (1,1) is always zero (G is skew-symmetric).
1 3 8.326474500954891E-003 <- A_{up,up}, triplet
1 4 -0.228326252284219 <- A_{up,up}, triplet
1 5 0.470855192339553 <- A_{up,up}, triplet
1 6 -3.285258904186700E-002 <- A_{up,up}, triplet
1 7 -5.097409720647310E-003 <- A_{up,up}, triplet
1 8 5.679495868355650E-002 <- A_{up,up}, triplet
1 9 0.684164602152446 <- A_{up,dn}, singlet
...
1 16 -0.104285811627841 <- A_{up,dn}, singlet
2 3 -2.076224374212450E-002 <- A_{up,up}, triplet
...
2 8 -4.145465677435435E-003 <- A_{up,up}, triplet
2 9 3.735515724267560E-003 <- A_{up,dn}, triplet
2 10 0.520587530210701 <- A_{up,dn}, singlet
...
2 16 4.428757569068110E-003 <- A_{up,dn}, singlet
...
9 10 4.813787735439980E-003 <- A_{dn,dn}, triplet
...
15 16 9.827312227017149E-003 <- A_{dn,dn}, triplet
```

From index 1 to 8 -> spin-up  
 From index 9 to 16 -> spin-dn

$$A = \begin{bmatrix} A_{\text{up-up}} & A_{\text{up-dn}} \\ A_{\text{dn-up}} & A_{\text{dn-dn}} \end{bmatrix}$$

$$f(\mathbf{r}_i, \mathbf{r}_j) = \sum_{l,m,a,b} A_{\{a,l\},\{b,m\}} \psi_{a,l}(\mathbf{r}_i) \psi_{b,m}(\mathbf{r}_j)$$

We have 4 basis for each C atoms.  
 => 16 \* 16 matrix

$$A_{\text{up-up}} = \begin{pmatrix} 0 & A_{1,2} & \dots & A_{1,8} \\ -A_{1,2} & 0 & \dots & A_{2,8} \\ \vdots & \vdots & \ddots & \vdots \\ -A_{1,8} & -A_{2,8} & \dots & 0 \end{pmatrix}$$

$$A_{\text{dn-dn}} = \begin{pmatrix} 0 & A_{9,10} & \dots & A_{9,16} \\ -A_{9,10} & 0 & \dots & A_{10,16} \\ \vdots & \vdots & \ddots & \vdots \\ -A_{9,16} & -A_{10,16} & \dots & 0 \end{pmatrix}$$

## The most general paring function (Pfaffian ansatz).

```
This is a C2-dimer case
The number of basis set for each carbon is 4
Nonzero values of detmat
1 2 -2.917621798712210E-002 <- (1,1) is always zero (G is skew-symmetric).
1 3 8.326474500954891E-003 <- A_{up,up}, triplet
1 4 -0.228326252284219 <- A_{up,up}, triplet
1 5 0.470855192339553 <- A_{up,up}, triplet
1 6 -3.285258904186700E-002 <- A_{up,up}, triplet
1 7 -5.097409720647310E-003 <- A_{up,up}, triplet
1 8 5.679495868355650E-002 <- A_{up,up}, triplet
1 9 0.684164602152446 <- A_{up,dn}, singlet
...
1 16 -0.104285811627841 <- A_{up,dn}, singlet
2 3 -2.076224374212450E-002 <- A_{up,up}, triplet
...
2 8 -4.145465677435435E-003 <- A_{up,up}, triplet
2 9 3.735515724267560E-003 <- A_{up,dn}, triplet
2 10 0.520587530210701 <- A_{up,dn}, singlet
...
2 16 4.428757569068110E-003 <- A_{up,dn}, singlet
...
9 10 4.813787735439980E-003 <- A_{dn,dn}, triplet
...
15 16 9.827312227017149E-003 <- A_{dn,dn}, triplet
```

From index 1 to 8 -> spin-up

From index 9 to 16 -> spin-dn

$$A = \begin{bmatrix} A_{\text{up-up}} & A_{\text{up-dn}} \\ A_{\text{dn-up}} & A_{\text{dn-dn}} \end{bmatrix}$$

$$f(\mathbf{r}_i, \mathbf{r}_j) = \sum_{l,m,a,b} A_{\{a,l\},\{b,m\}} \psi_{a,l}(\mathbf{r}_i) \psi_{b,m}(\mathbf{r}_j)$$

We have 4 basis for each C atoms.  
=> 16 \* 16 matrix

$$A_{\text{up-dn},S} = \begin{pmatrix} A_{1,9} & A_{1,10} & \dots & A_{1,16} \\ A_{2,10} & \dots & A_{2,16} \\ \ddots & \ddots & \vdots \\ & & A_{8,16} \end{pmatrix}$$

$$A_{\text{up-dn},T} = \begin{pmatrix} 0 & -A_{2,9} & \dots & -A_{8,9} \\ A_{2,9} & 0 & \dots & -A_{8,10} \\ \vdots & \vdots & \ddots & \vdots \\ A_{8,9} & A_{8,10} & \dots & 0 \end{pmatrix}$$

## Coefficients of the Jastrow part (spin-independent Jastrow)

```
Nonzero values of jasmat
1 1 8.971451176330450E-009
1 2 9.853858918304112E-002
2 2 9.703779722477737E-002
```

$$J_{3/4}(\mathbf{r}_1\sigma_1, \dots, \mathbf{r}_N\sigma_N) = \sum_{i < j} \left( \sum_{a,l} \sum_{b,m} M_{a,l,b,m}^{\sigma_i, \sigma_j} \chi_{a,l}(\mathbf{r}_i) \chi_{b,m}(\mathbf{r}_j) \right),$$

```
...
1 45 -2.042711544366610E-004
1 91 -6.994272320227231E-004 <- inhomogeneous onebody M.
```

$$J_1^{inh}(\mathbf{r}_1\sigma_1, \dots, \mathbf{r}_N\sigma_N) = \sum_{i=1}^N \sum_{a=1}^{N_{\text{at}}} \left( \sum_l M_{a,l}^{\sigma_i} \chi_{a,l}(\mathbf{r}_i) \right)$$

twobody: 1B and 2B Jastrows:    Various Jastrow types are implemented (see the manual.)

Typically:

-6: Open/PBC with pseudo potentials

-22: Open/PBC with JAGPu/JPf.

Only two-body parameter.  $1b = \frac{1}{2a}(1 - e^{-ar})$

i.e., electron-ion cusp conditions are enough.

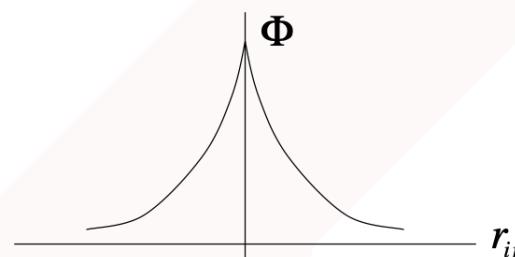
Only one-body or two-body and one-body parameters.

Spin-dependent Jastrow factors:

-15: Open/PBC with all-electrons

two-body and one-body parameters.

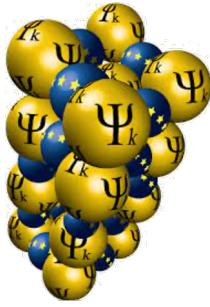
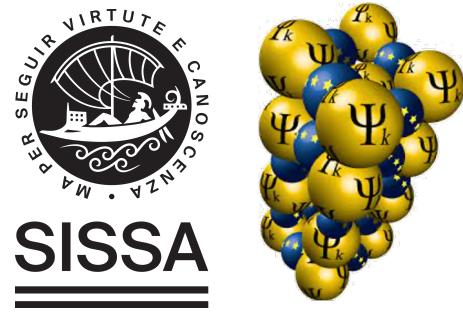
$$2b = \frac{r}{2(1 + br)} \quad 1b = \frac{1}{2b}(1 - e^{-br})$$



Electron-ion (1b).

Electron-Electron (2b).

To satisfy the cusp conditions.



## Day2:

- Various ansatz (JDFT/JsAGPs/JAGPu/JAGP)
- **Wavefunction conversion**
- Wavefunction optimization



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## Conversion tools (convertfort10.x, convertpfaff)

Input: convertfort.input,  
fort.10\_in, fort.10\_out

Binary: convertfort10.x

Output:fort10\_new

Convergfort10.x is a tool for converting a WF type., e.g.,

JSD

JAGPs

JAGPu

Input: fort.10\_in,  
fort.10\_out

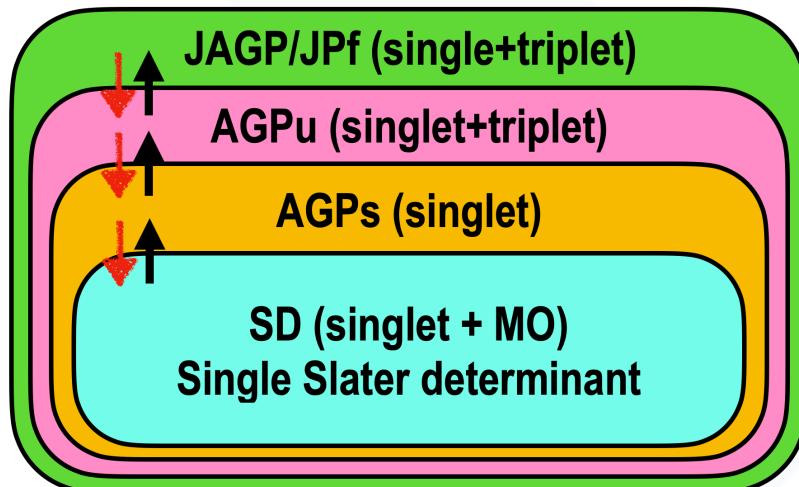
Binary: convertfortpfaff.x

Output:fort10\_new

Convertpfaff.x is a tool for projecting a WF., e.g.,

JAGPu

JAGP/JPf



→ Conversion (no loss of information)

→ Projection (loss of information)

Hybrid orbitals (90000): In fort.10, 900000 indicates a hybrid orbital.

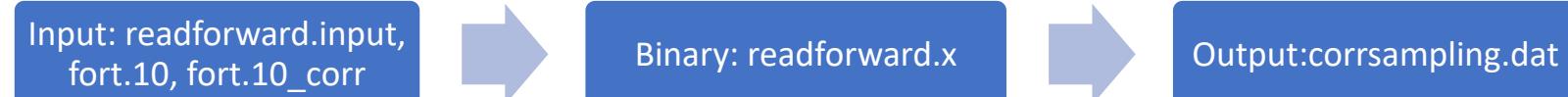
```
#atom index, the number of components, 900000
#index of basis [1,2,...]
#coefficients for basis [1,2,...]
 1 90 900000
 1 1 2 3 4 5
 6 7 8 9 10 11
12 13 14 15 16 17
18 19 20 21 22 23
24 25 26 27 28 29
30 31 32 33 34 35
36 37 38 39 40 41
42 43 44 45 4.415629124781804E-004
-2.665471779107012E-003 6.462432564128138E-003 -2.835419348050690E-002
-1.801631060924397E-003 0.000000000000000E+000 0.488607316300470
-1.08438499459258 1.000000000000000E+000 -8.862166918962697E-002
-3.585186058053676E-006 1.336604741376926E-005 -1.034531513737405E-002
-9.682848944243672E-005 7.780031865084339E-005 -2.330742724611005E-002
2.406091695918141E-004 -1.314165271323025E-004 -1.383980745357883E-002
-8.265782808695380E-005 6.484551172622954E-005 -6.461899158835088E-002
-1.224707476287876E-003 3.784895470189310E-004 -0.150215939301643
3.279641185411990E-003 4.146447536354074E-004 -5.370349262603082E-002
-2.867011651206949E-003 -6.433419048360544E-004 -0.169339132045330
0.000000000000000E+000 0.000000000000000E+000 5.388221636070670E-002
3.865987502185416E-004 1.537139475756473E-004 -0.134079774055112
-4.310821717930281E-004 -2.609351310060059E-004 2.739963165919702E-002
2.693581696773797E-002 -3.679623706959143E-005 1.393726496455493E-004
-1.728876043016380E-004 1.648834534792205E-004
```

|                                                                                                                |                          |
|----------------------------------------------------------------------------------------------------------------|--------------------------|
| <pre>ATOM_6 &amp;shells nshelldet=18 nshelljas=10 ndet_hyb=4 / 1   1   16 1   13.073594000000 1   1   16</pre> | <b>makefort.10.input</b> |
|----------------------------------------------------------------------------------------------------------------|--------------------------|

$$\tilde{\Phi}_k^a = \sum_i^{N_{basis}^a} c_{i,k}^a \cdot \phi_i^a (\mathbf{r})$$

$sp^2$ ,  $sp^3$ , etc...

Hybrid orbitals can be added by “convertfort10.x”. We can decrease the number of variational parameters.



readforward.x enables us to calculate the difference in two WF using the correlated sampling.

JSD  $\longleftrightarrow$  JAGPs

- The difference in energies
- The Overlap between the two WFs  
(the maximum is unity)

```
%cat corrsampling.dat
```

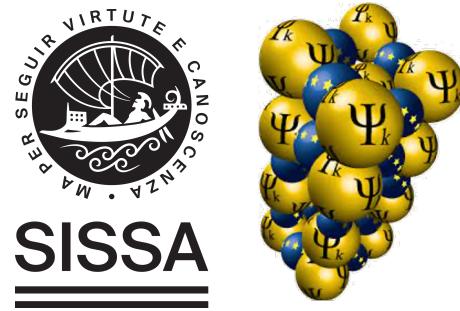
reference energy: E(fort.10) -0.110045875E+02 0.252368934E-01

reweighted energy: E(fort.10\_corr) -0.110045875E+02 0.252368985E-01

reweighted difference: E(fort.10)-E(fort.10\_corr) -0.148834687E-07 0.316227766E-07

Overlap square : (fort.10,fort.10\_corr) 0.999999998E+00 0.316227766E-07

If the overlap is unity, it means that the conversion has been done without losing any information.

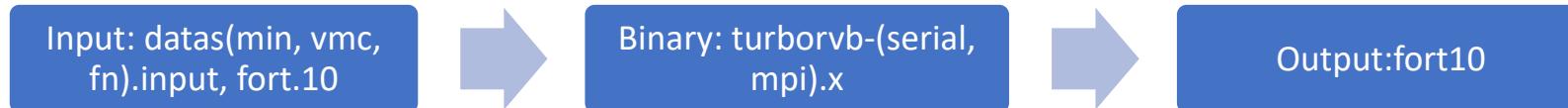


## Day2:

- Various ansatz (JDFT/JsAGPs/JAGPu/JAGP)
- Wavefunction conversion
- **Wavefunction optimization**



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turborvb.x is the main QMC engine in the turborvb package.

=VMC-opt, VMC, DMC, and LRDMC=

- Single-shot VMC run (itestr4=-2 in the &simulation namelist).
- VMC optimization (itestr4=-4,-5,-8,-9 in the &simulation namelist).
- Single-shot LRDMC run (itestr4=-6 in the &simulation namelist).
- Single-shot DMC run (itestr4=-5 in the &simulation namelist), but not maintained.

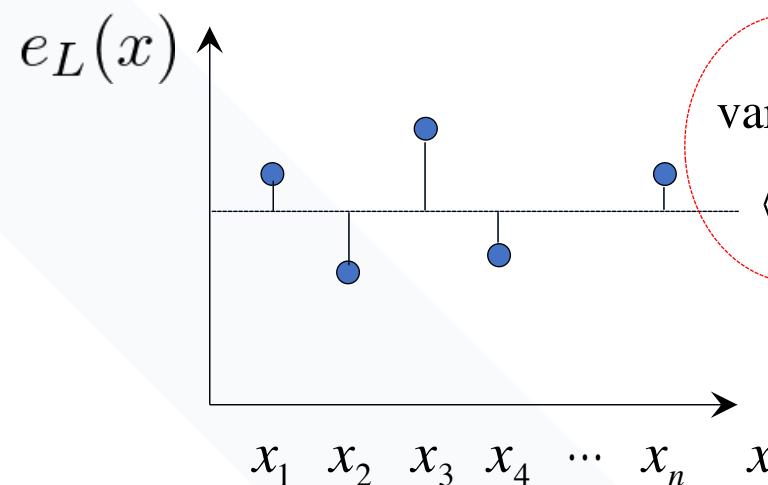
```

&simulation
 itest4=-4
 ngen=10000
 iopt=1
 maxtime=10800
/
&pseudo
/
&vmc
 epscut=0.0
/
&optimization
 nweight=100
 nbinsr=5
 iboot=0
 tpar=0.35
 parr=-0.001
/
&readio
 !iread=3
/
¶meters
 !iessw=1
 !iesup=1
 !iesm=1
 !ieskin=1
 iesd=1
 iesfree=1
/

```

## Relation between ngen and nweight

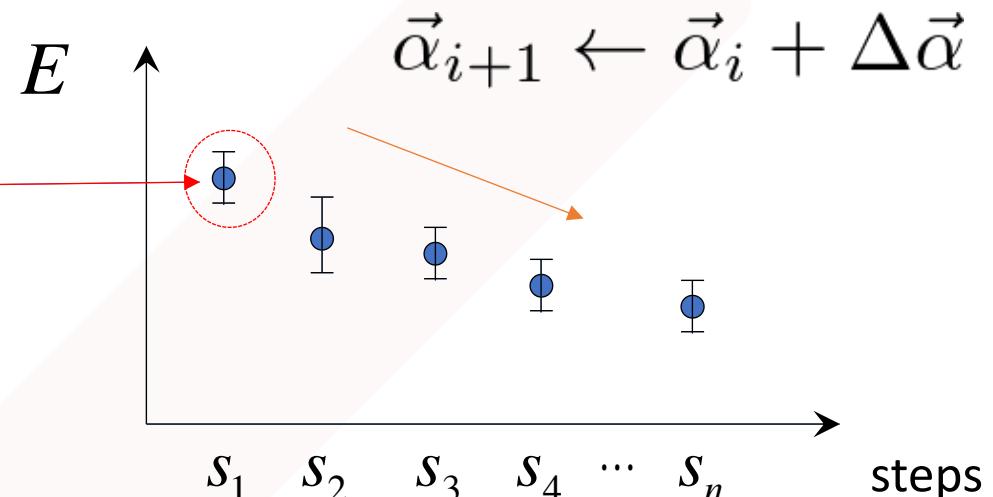
Each iteration



||  
nweight × nw

(default: the num. walker = the num. of MPI process )

Optimization



Total optimization steps:  $\frac{\text{ngen}}{\text{nweight}}$

## Implemented optimization algorithms

-9, -5): Stochastic reconfiguration (natural gradient method)

S Sorella, et al., *J. Chem. Phys.* 127, 014105 (2007).

-4, -8): Linear method with the natural gradient

C.J. Umrigar, et al., *Phys. Rev. Lett.* 98, 110201 (2007).

In both cases, the most important parameters in practice are

1. tpar: Acceleration parameter (learning rate.)

e.g.,  $\alpha_k \rightarrow \alpha_k + \Delta \cdot (\mathcal{S}'^{-1} \mathbf{f})_k$       tpar = 3.5d-1, and 1.0d-3 for -4 and -9, respectively.

2. parr: Regularization (c.f. LASSO)

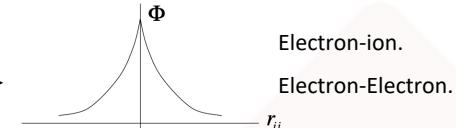
e.g.,  $s'_{i,i} = s_{i,i}(1 + \varepsilon)$

Depending on the accuracy you need. parr = ~ 1.0d-3

### 3. VMC Optimize wavefunctions and VMC run.

A wavefunction reads  $\Psi_{AS}(\vec{R}) \times \exp(J(\vec{R})) \longrightarrow$

Anti-symmetric part. Jastrow factor.



To satisfy the cusp.

Jastrow factor =  $\exp(J(\vec{R}))$  No effect on the nodal surface!!  $\Psi(\vec{R}) \equiv \Psi(\vec{r}_1, \vec{r}_2, \dots, \vec{r}_N) = 0$

Anti-symmetric part =  $\Psi_{AS}(\vec{R})$  Determines the nodal surface. Its initial guess is taken from a DFT calculation!!

TurboRVB:

Both parts are optimized.

Stable nodal surface optimization

Independent of an initial DFT guess!?



Other QMC codes:

Only the Jastrow part is optimized.

Unstable nodal surface optimization

Dependent on an initial DFT guess!!

e.g., however, the optimization sometimes is stuck in a local minimum if the initialization was wrong etc...

Practical recommended optimization procedure.

Avoid local minima...

**1. Put a reasonable two-body Jastrow parameter (typically  $\sim 1.0$  for twobody = -6, -15, -22),**

%vi fort.10

**2. Optimize homogenous and inhomogeneous one-body Jastrows (two-body and three-body are fixed),**

iesfree=1, iesd=1 in the &parameters section.

twobodyoff=.true. and iesdtwobodyoff=.true. in the &optimization section.

**3. Optimize three-body Jastrow part (two-body still fixed),**

Remove !twobodyoff=.true.

**4. Optimize two-body Jastrow part.**

remove !twobodyoff=.true. and !iesdtwobodyoff=.true.

The other options

iessw=1 Opt. the determinant part.

iesup=1 Opt. the hyb. orbitals. / itestr4=-9/-4

+ Opt. the exponents (Det). / itestr4=-8/-5

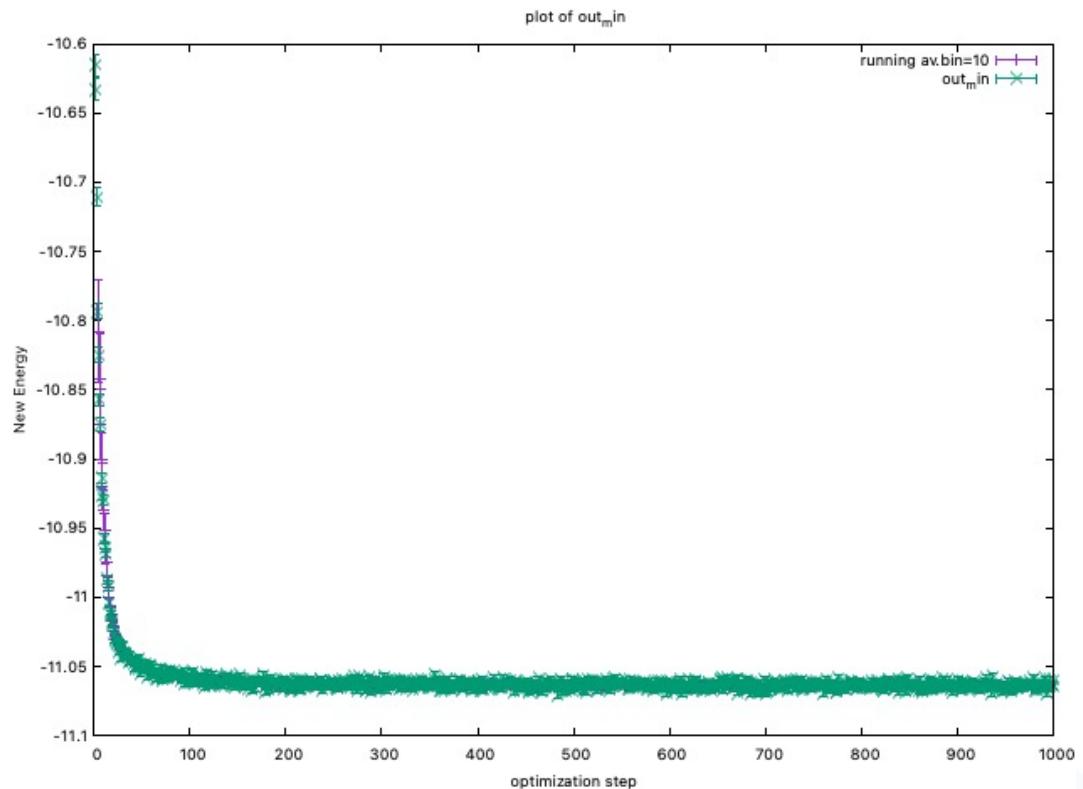
iesm=1 Opt. the exponents (Jas).

## Optimization criteria

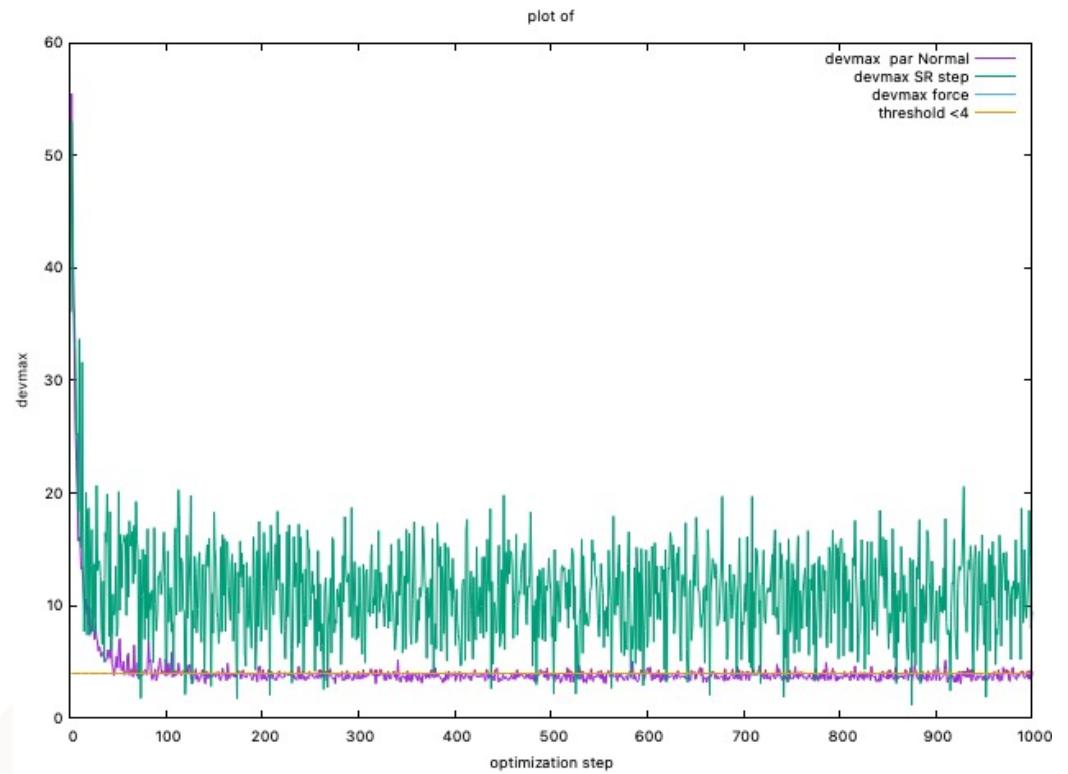
At least, ``devmax`` should be smaller than 4.0 after optimization. However, we also have experienced that this simple criteria is sometimes not sufficient to obtain a converged result.

The definition of ``devmax`` is:  $devmax \equiv \max_k \left( \left| \frac{f_k}{\sigma_{f_k}} \right| \right)$

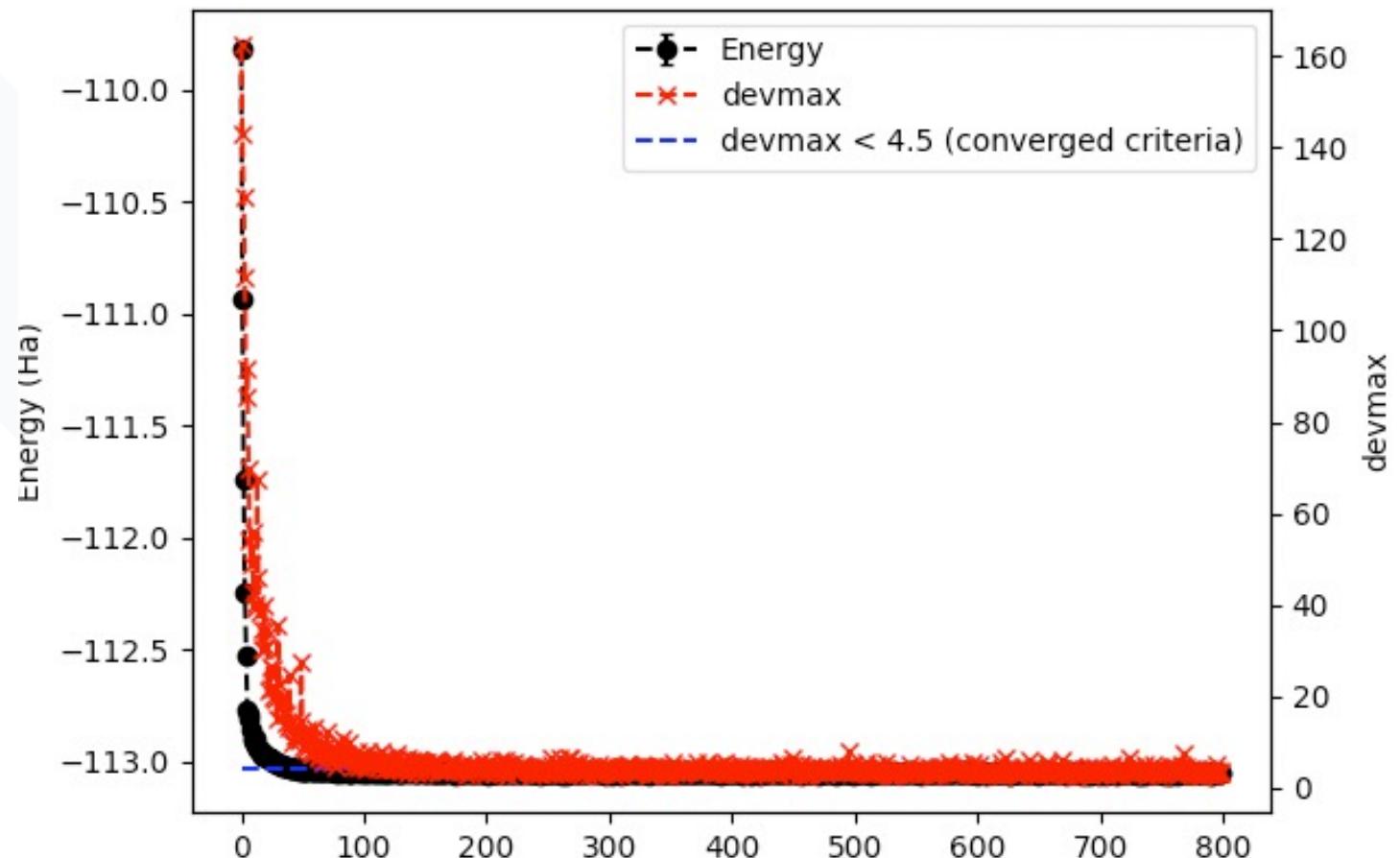
where  $\sigma_{f_k}$  represents the estimated error bar of a general force  $f_k = -\frac{\partial E(\alpha)}{\partial \alpha_k} = -\frac{\partial}{\partial \alpha_k} \frac{\langle \Psi_\alpha | \hat{\mathcal{H}} | \Psi_\alpha \rangle}{\langle \Psi_\alpha | \Psi_\alpha \rangle}$ .



plot\_Energy.sh

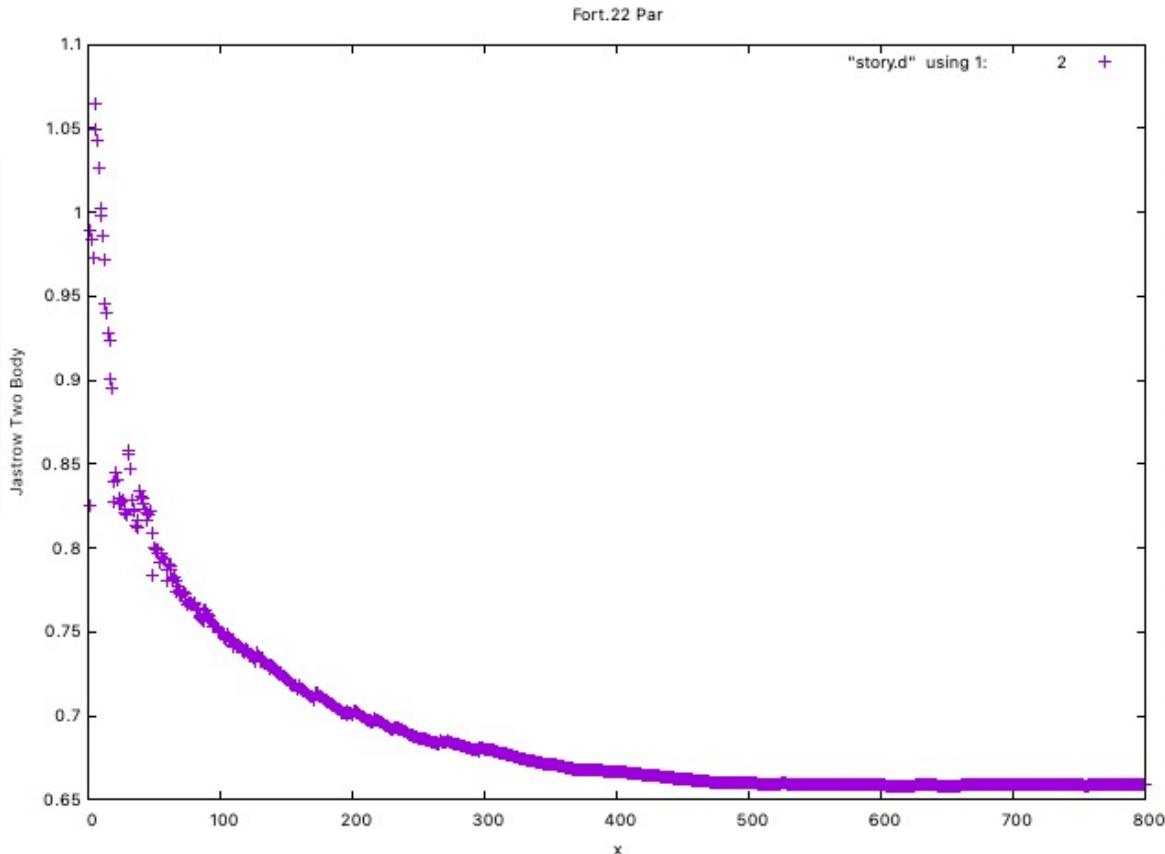


plot\_devmax.sh



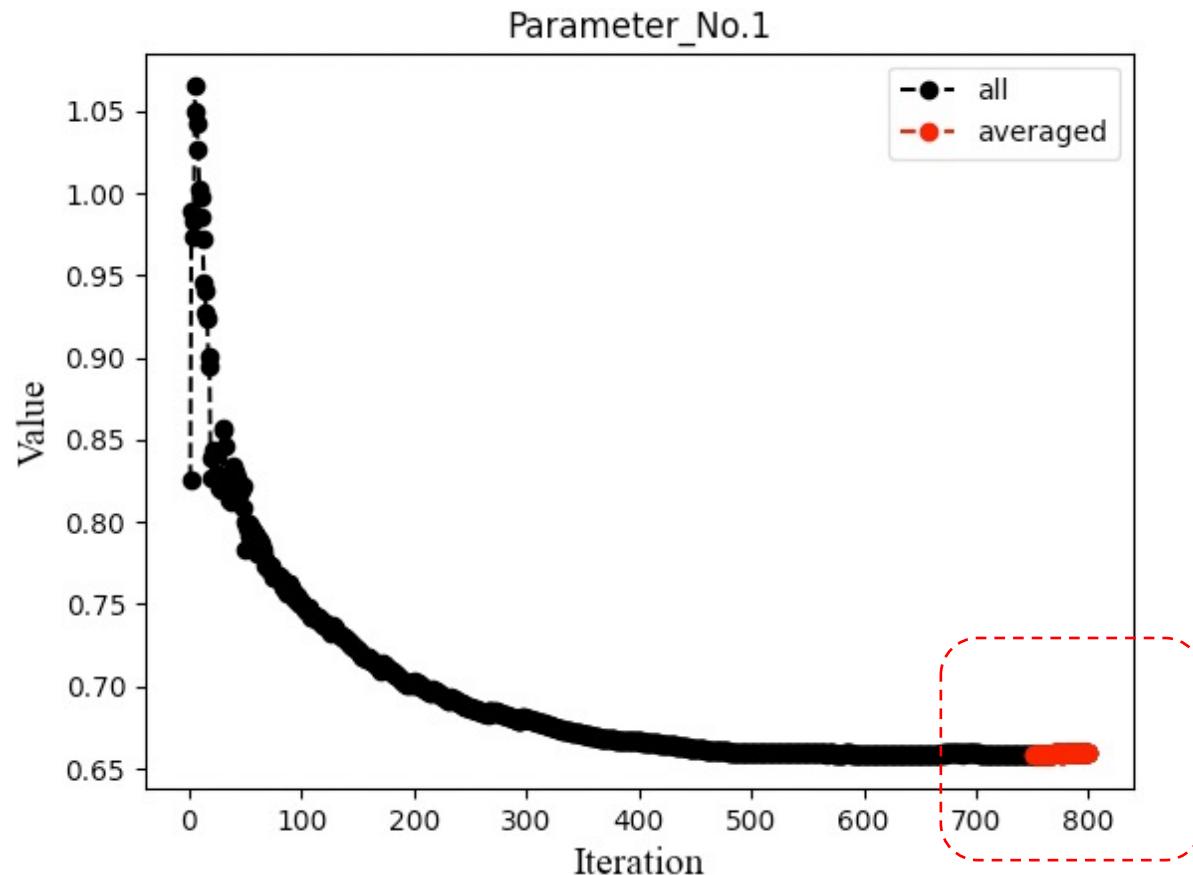
```
%turbo-genius.sh -j vmcopt -post -am interactive_detail
```

readalles.x enables us to visualize and average the latest several optimization steps.



% cat read.in  
1 1 0 1  
0  
10

% readalles.x < read.in

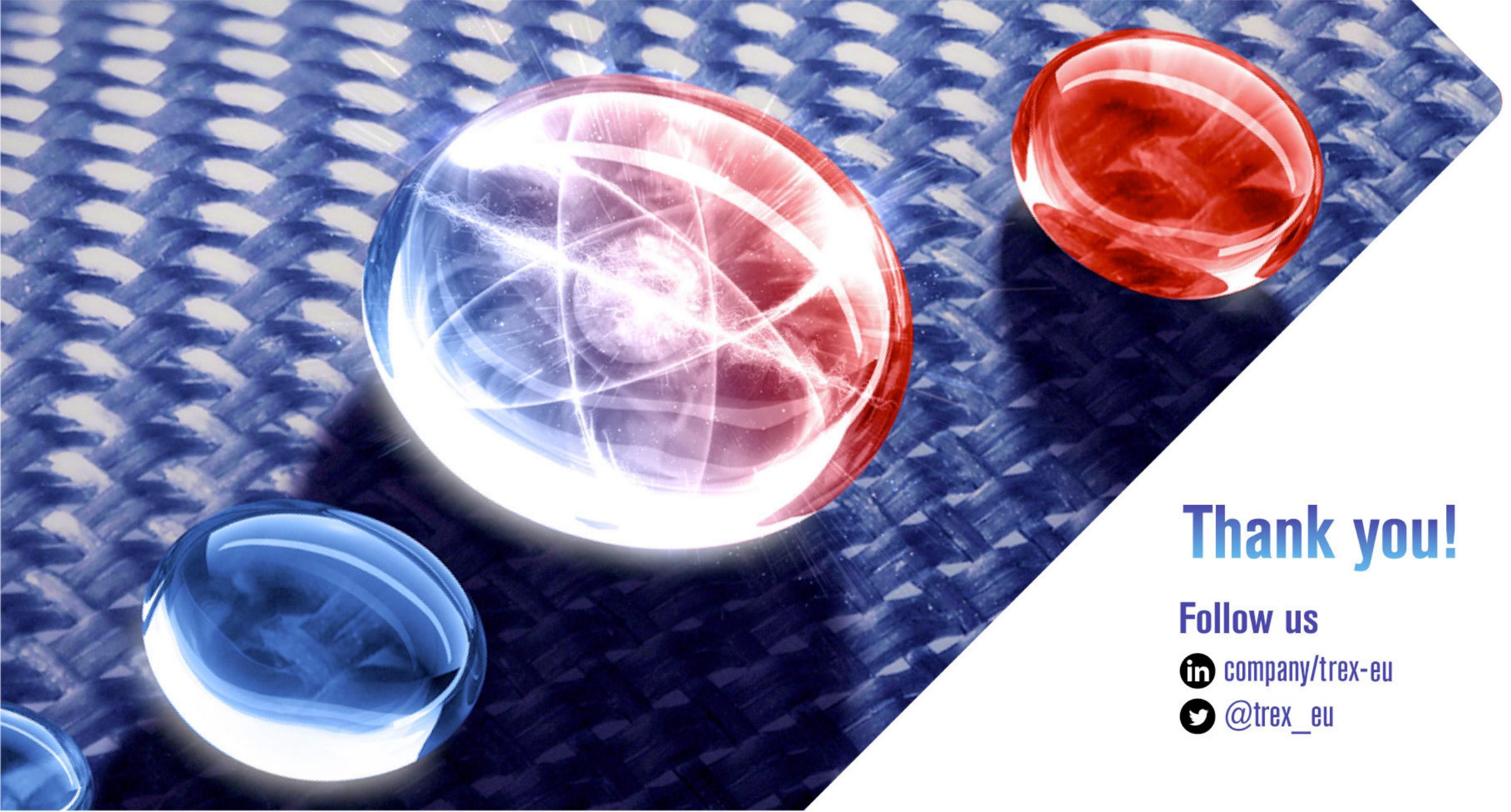


Averaged!

turbo-genius.sh -j vmcopt -post -am interactive\_detail

## Ansatz Level

|                                        |                                 | JDFT                          |                          |                      |                      | JsAGPs                 |                         |                      |                      | JAGPu                         |                        |                         |                      | JAGP(JPf)            |                        |                       |                      |                      |  |  |  |  |
|----------------------------------------|---------------------------------|-------------------------------|--------------------------|----------------------|----------------------|------------------------|-------------------------|----------------------|----------------------|-------------------------------|------------------------|-------------------------|----------------------|----------------------|------------------------|-----------------------|----------------------|----------------------|--|--|--|--|
| 1.<br>H <sub>2</sub> -dimer            | H <sub>2</sub>                  | 01<br>DFT<br>Day1             | 02<br>VMCo<br>Day2,3     | 03<br>VMC<br>Day3    | 04<br>DMC<br>Day4    | 06<br>Conv.<br>Day2    | 08<br>VMCo<br>Day2,3    | 09<br>VMC<br>Day3    | 10<br>DMC<br>Day4    | NA                            |                        |                         |                      | NA                   |                        |                       |                      |                      |  |  |  |  |
| 2.<br>C <sub>2</sub> -dimer            | C <sub>2</sub>                  | 01-01<br>01-05<br>DFT<br>Day1 | 01-06<br>VMCo<br>Day2,3  | 01-07<br>VMC<br>Day3 | 01-08<br>DMC<br>Day4 | 02-01<br>Conv.<br>Day2 | 02-02<br>VMCo<br>Day2,3 | 02-03<br>VMC<br>Day3 | 02-04<br>DMC<br>Day4 | 03-01<br>03-03<br>DFT<br>Day1 | 03-04<br>Conv.<br>Day2 | 03-05<br>VMCo<br>Day2,3 | 03-06<br>VMC<br>Day3 | 03-06<br>DMC<br>Day4 | 04-01<br>Conv.<br>Day3 | 04-03<br>VMCo<br>Day4 | 04-03<br>VMC<br>Day4 | 04-03<br>DMC<br>Day4 |  |  |  |  |
|                                        | C                               | Day1                          | Day2,3                   | Day3                 | Day4                 |                        |                         |                      |                      | 03-01<br>DFT<br>Day1          |                        |                         |                      |                      | 04-02<br>Conv.<br>Day3 |                       |                      |                      |  |  |  |  |
| 3.<br>H <sub>2</sub><br>on<br>graphene | H <sub>2</sub><br>+<br>Graphene | 01<br>DFT<br>Day1             | 02<br>VMCo<br>Day2,3     | 03<br>VMC<br>Day3    | 04<br>DMC<br>Day4    | NA                     |                         |                      |                      | NA                            |                        |                         |                      | NA                   |                        |                       |                      |                      |  |  |  |  |
|                                        | Graphene                        | 05<br>DFT<br>Day1             | 06<br>VMCo<br>Day2,3     | 07<br>VMC<br>Day3    | 08<br>DMC<br>Day4    |                        |                         |                      |                      |                               |                        |                         |                      |                      |                        |                       |                      |                      |  |  |  |  |
|                                        | H <sub>2</sub>                  | 09<br>DFT<br>Day1             | 10<br>VMCo<br>Day2,<br>3 | 11<br>VMCo<br>Day3   | 12<br>DMC<br>Day4    |                        |                         |                      |                      |                               |                        |                         |                      |                      |                        |                       |                      |                      |  |  |  |  |



# Thank you!

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